

15

I.

EVALUATING STATEMENTS Decide whether the statement is *always*, *sometimes*, or *never* true.

14. If $m\angle 1 = 40^\circ$, then $m\angle 2 = 140^\circ$. **N**

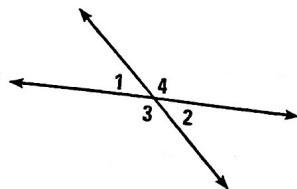
15. If $m\angle 4 = 130^\circ$, then $m\angle 2 = 50^\circ$. **A**

16. $\angle 1$ and $\angle 4$ are congruent. **S**

17. $m\angle 2 + m\angle 3 = m\angle 1 + m\angle 4$. **A**

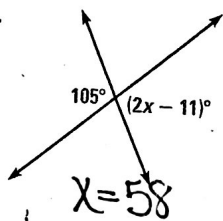
18. $\angle 2 \cong \angle 1$. **A**

19. $m\angle 2 = 90^\circ - m\angle 3$. **N**



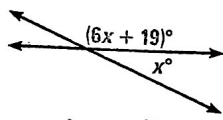
20. USING ALGEBRA Find the value(s) of the variable(s).

28.



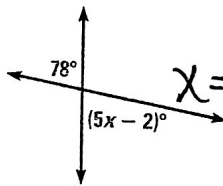
$x = 58$

29.



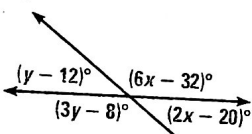
$x = 23$

30.



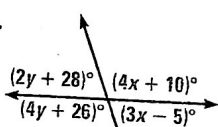
$x = 16$

31.



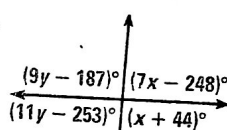
$x = 29, y = 50$

32.



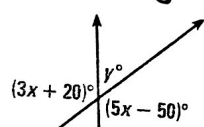
$x = 25, y = 21$

33.



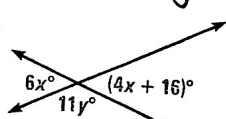
$x = 48, y = 31$

34.



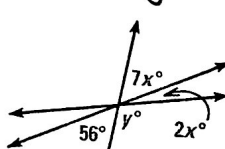
$x = 35, y = 55$

35.



$x = 8, y = 12$

36.

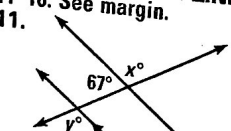


$x = 8, y = 108$

II.

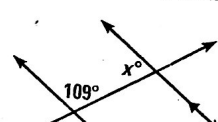
USING PARALLEL LINES Find the values of x and y . Explain your reasoning.

11.



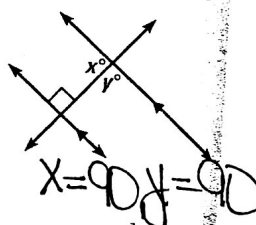
$x = 113, y = 113$

12.



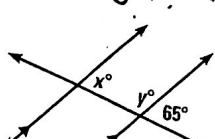
$x = 71, y = 109$

13.



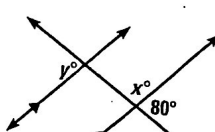
$x = 90, y = 90$

14.



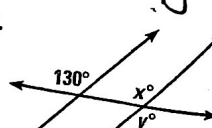
$x = 65, y = 115$

15.



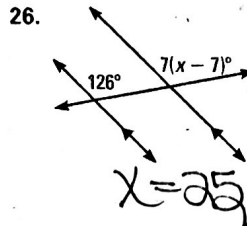
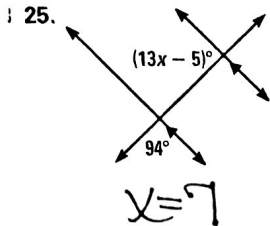
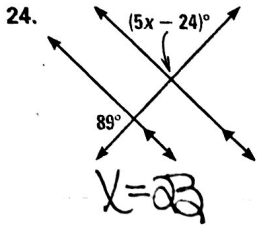
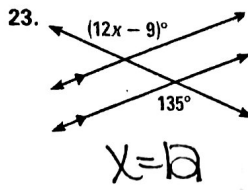
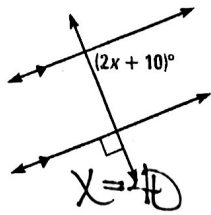
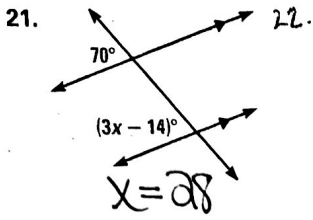
$x = 100, y = 80$

16.



$x = 130, y = 130$

20. USING ALGEBRA Find the value of x .



Lesson 1

- I. 14) Never - vertical \angle 's are \cong
 15) Always - linear pair \angle 's are supplementary
 16) Sometimes - linear pair \angle 's could be \cong if both were 90°
 17) Always - linear pair \angle 's are supplementary \therefore sum is 180°
 18) Always - vertical \angle 's are \cong
 19) Never - linear pair \angle 's are supplementary $\therefore m\angle 2 = 180^\circ - m\angle 1$

28) Vertical \angle 's \cong
 $105 = 2x - 11$
 $116 = 2x$
 $58 = x$

29) linear pair supple.
 $6x + 19 + x = 180$
 $7x = 161$
 $x = 23$

30) Vertical \angle 's \cong
 $78 = 5x - 2$
 $80 = 5x$
 $16 = x$

31) linear pair supple.
 $6x - 32 + 2x - 20 = 180$ } $y - 12 + 3y - 8 = 180$
 $8x - 52 = 180$ } $4y - 20 = 180$
 $8x = 232$ } $4y = 200$
 $x = 29$ } $y = 50$

32) linear pair supple.
 $4x + 10 + 2x - 5 = 180$ } $2y + 28 + 4y + 26 = 180$
 $7x + 5 = 180$ } $6y + 54 = 180$
 $7x = 175$ } $6y = 126$
 $x = 25$ } $y = 21$

33) linear pair supple.
 $7x - 248 + x + 44 = 180$ } $9y - 187 + 11y - 253 = 180$
 $8x - 204 = 180$ } $20y - 440 = 180$
 $8x = 384$ } $20y = 620$
 $x = 48$ } $y = 31$

34) Vert \angle 's \cong } linear pair supple.
 $3x + 20 = 5x - 50$ } $3x + 20 + y = 180$
 $70 = 2x$ } $105 + 20 + y = 180$
 $35 = x \rightarrow$ } $675 + y = 180$
 $y = 55$

35) Vertical \angle 's \cong } linear pair supple.
 $6x = 4x + 16$ } $6x + 11y = 180$
 $2x = 16$ } $48 + 11y = 180$
 $x = 8 \rightarrow$ } $11y = 132$
 $y = 12$

36) Vertical \angle 's \cong } Adjacent \angle 's that form a straight line add up to 180°
 $56 = 7x$
 $8 = x$
 $7x + 2x + y = 180$
 $7(8) + y = 180$
 $56 + y = 180$
 $y = 124$

II 11) linear pt. supple. $\left\{ \begin{array}{l} \text{Alt. ext. } \angle's \cong \\ 67 + x = 180 \\ x = 113 \end{array} \right. \rightarrow 113 = y$ 12) Vert. $\angle's \cong \left\{ \begin{array}{l} \text{same side int. } \\ \angle's \text{ supple.} \\ y = 109 \\ x + 109 = 180 \\ x = 71 \end{array} \right.$

13) same side int. $\angle's$ supple. $\left\{ \begin{array}{l} \text{Alt. int. } \angle's \cong \\ y = 90 \\ x + 90 = 180 \\ x = 90 \end{array} \right.$ 14) linear pt. supple. $\left\{ \begin{array}{l} \text{same side int. } \\ \angle's \text{ supple.} \\ y + 65 = 180 \\ y = 115 \end{array} \right. \rightarrow \left\{ \begin{array}{l} x + y = 180 \\ x + 115 = 180 \\ x = 65 \end{array} \right.$

15) linear pt. supple. $\left\{ \begin{array}{l} \text{Alt. ext. } \angle's \cong \\ x + 80 = 180 \\ x = 100 \\ y = 80 \end{array} \right.$ 16) corresponding $\angle's \cong \left\{ \begin{array}{l} \text{Vertical } \angle's \cong \\ x = y \\ 130 = x \rightarrow 130 = y \end{array} \right.$

a) corresponding $\angle's \cong$
 $70 = 3x - 14$
 $84 = 3x$
 $28 = x$

a) vertical $\angle's \cong$, then same side int. $\angle's$ are supple.
 $2x + 10 + 90 = 180$
 $2x + 100 = 180$
 $2x = 80 \quad x = 40$

a) alt. ext. $\angle's$ are \cong
 $12x - 9 = 135$
 $12x = 144$
 $x = 12$

a) vertical $\angle's \cong$, then same side int. $\angle's$ are supple.
 $5x - 24 + 89 = 180$
 $5x + 65 = 180$
 $5x = 115$
 $x = 23$

a) vertical $\angle's \cong$, then same side int. $\angle's$ are supple.
 $13x - 5 + 94 = 180$
 $13x + 89 = 180$
 $13x = 91$
 $x = 7$

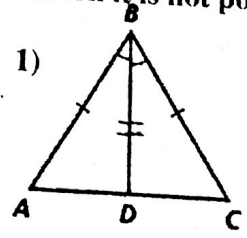
a) corresponding $\angle's$ are \cong
 $7(x - 7) = 126$
 $7x - 49 = 126$
 $7x = 175$
 $x = 25$

Geometry
Worksheet - Congruent Triangles

NAME Keya

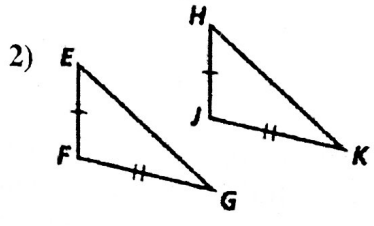
Date _____ HR _____

- a) Determine whether the following triangles are congruent.
- b) If they are, name the triangle congruence (pay attention to proper correspondence when naming the triangles) and then identify the Theorem or Postulate (SSS, SAS, ASA, AAS, HL) that supports your conclusion.
- c) Be sure to show any additional congruence markings you used in your reasoning.
- d) If the triangles cannot be proven congruent, state "not possible." Then given the reason it is not possible.



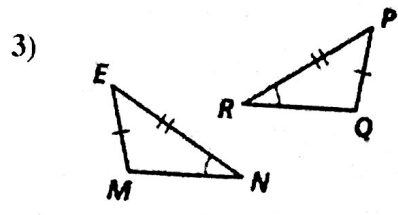
Congruence:
 $\triangle ABD \cong \triangle CBD$

Reason: SAS



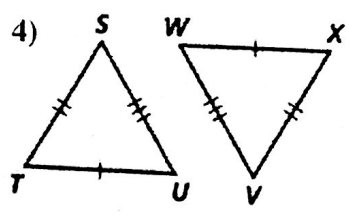
Congruence:
 $\triangle EFG \cong \triangle$ _____

Reason: Not possible



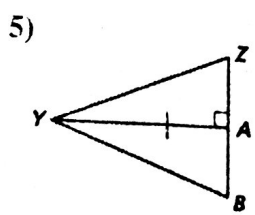
Congruence:
 $\triangle EMN \cong \triangle$ _____

Reason: Not possible
SAS is not a way to prove \triangle 's \cong



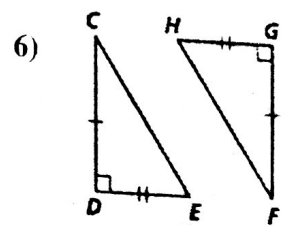
Congruence:
 $\triangle STU \cong \triangle VWX$

Reason: SSS



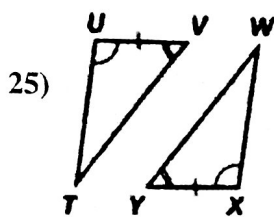
Congruence:
 $\triangle YZA \cong \triangle$ _____

Reason: Not possible



Congruence:
 $\triangle CDE \cong \triangle FGH$

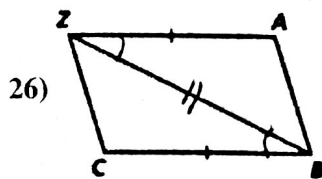
Reason: SAS



Congruence:

$\Delta TUV \cong \Delta WXY$

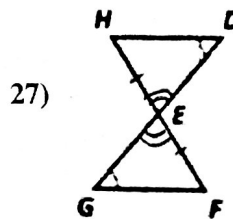
Reason: ASA



Congruence:

$\Delta ABCZ \cong \Delta$ Not possible

Reason:

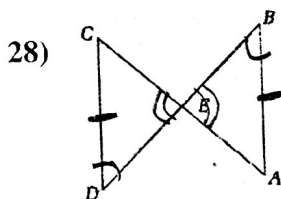


Congruence:

$\Delta EFG \cong \Delta EDH$

Reason: ASA

Use the given information to mark the diagram appropriately. Name the triangle congruence (pay attention to proper correspondence when naming the triangles) and then identify the Theorem or Postulate (SSS, SAS, ASA, AAS, HL) that would be used to prove the triangles congruent. If the triangles cannot be proven congruent, state "not possible."

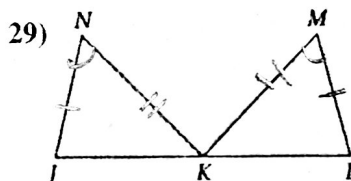


Given: $\overline{CD} \cong \overline{AB}$; $\angle B \cong \angle D$

Congruence:

$\Delta CDE \cong \Delta ABE$

Reason: SAS

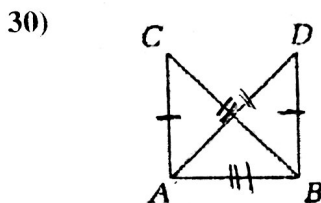


Given: $\overline{JN} \cong \overline{LM}$; $\overline{NK} \cong \overline{MK}$;
 $\angle N \cong \angle M$

Congruence:

$\Delta JKN \cong \Delta LKM$

Reason: SAS

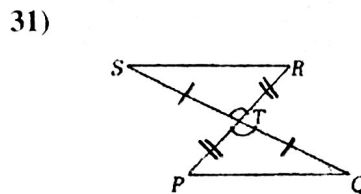


Given: $\overline{AC} \cong \overline{BD}$; $\overline{AD} \cong \overline{BC}$

Congruence:

$\Delta ABC \cong \Delta BAD$

Reason: SSS



Given: \overline{SQ} and \overline{PR} bisect each other

Congruence:

$\Delta RST \cong \Delta PQT$

Reason: SAS